

Exam 3 Review: Modules 5

Name_____

SHORT ANSWER. Write the word or phrase that best completes each statement or answers the question.

Factor out the GCF from the polynomial.

1) $12m^8 - 60m^4 + 54m^2$

Answer: $6m^2(2m^6 - 10m^2 + 9)$

1) _____

2) $48x^8y^7 + 160x^6y^5 - 32x^3y^2$

Answer: $16x^3y^2(3x^5y^5 + 10x^3y^3 - 2)$

2) _____

3) $32x^8y^8 - 40x^2y^6 - 64x^5y^3$

Answer: $8x^2y^3(4x^6y^5 - 5y^3 - 8x^3)$

3) _____

4) $32p + 8q - 8$

Answer: $8(4p + q - 1)$

4) _____

Factor the four-term polynomial by grouping.

5) $6x^4 + 8x^2 + 15x^2 + 20$

Answer: $(2x^2 + 5)(3x^2 + 4)$

5) _____

6) $15x^2 + 6xy - 25xy - 10y^2$

Answer: $(3x - 5y)(5x + 2y)$

6) _____

7) $15a^3 + 20a^2b - 9ab^2 - 12b^3$

Answer: $(5a^2 - 3b^2)(3a + 4b)$

7) _____

8) $20x^6 - 15x^3 - 8x^3 + 6$

Answer: $(5x^3 - 2)(4x^3 - 3)$

8) _____

Factor the trinomial completely. If the polynomial cannot be factored, write "prime."

9) $x^8 - 12x^4 + 35$

Answer: $(x^4 - 7)(x^4 - 5)$

9) _____

10) $x^2 + 10xy + 16y^2$

Answer: $(x + 2y)(x + 8y)$

10) _____

11) $u^2 - 6uv - 16v^2$

Answer: $(u + 2v)(u - 8v)$

11) _____

12) $x^2 + 4xy - 12y^2$

Answer: $(x + 6y)(x - 2y)$

12) _____

13) $4t^5 - 12t^4 - 40t^3$

Answer: $4t^3(t + 2)(t - 5)$

13) _____

14) $4r^6 - 8r^5 - 32r^4$

Answer: $4r^4(r + 2)(r - 4)$

14) _____

15) $-x^2 - 6x + 55$

Answer: $-1(x + 11)(x - 5)$

15) _____

16) $a^3b^2 - 9a^2b + 18a$

Answer: $a(ab - 3)(ab - 6)$

16) _____

Factor completely.

17) $15y^2 - 22y + 8$

Answer: $(3y - 2)(5y - 4)$

17) _____

18) $8z^2 - 6z - 9$

Answer: $(4z + 3)(2z - 3)$

18) _____

19) $12x^2 - 17xy + 6y^2$

Answer: $(4x - 3y)(3x - 2y)$

19) _____

20) $9x^2 + 6xy - 8y^2$

Answer: $(3x + 4y)(3x - 2y)$

20) _____

21) $49p^4 - 42p^3 + 9p^2$

Answer: $p^2(7p - 3)^2$

21) _____

22) $-2x^2 + 7x - 6$

Answer: $-1(2x - 3)(x - 2)$

22) _____

23) $84x^2 + 49xy + 7y^2$

Answer: $7(3x + y)(4x + y)$

23) _____

Factor the perfect square trinomial completely.

24) $25x^2 - 40xy + 16y^2$

Answer: $(5x - 4y)^2$

24) _____

25) $x^3 + 20x^2 + 100x$

Answer: $x(x + 10)^2$

25) _____

26) $32x^2 - 48xy + 18y^2$

Answer: $2(4x - 3y)^2$

26) _____

Factor the binomial completely.

27) $49x^2 - 9y^2$

Answer: $(7x + 3y)(7x - 3y)$

27) _____

28) $9a^3 - 4a$

Answer: $a(3a + 2)(3a - 2)$

28) _____

29) $98x^2y - 8y$

Answer: $2y(7x + 2)(7x - 2)$

29) _____

30) $64 - x^2y^2$

Answer: $(8 - xy)(8 + xy)$

30) _____

Solve the equation.

31) $x^2 + 8x - 33 = 0$

Answer: -11, 3

31) _____

32) $x^2 - x = 12$

Answer: -3, 4

32) _____

33) $x(5x + 28) = 12$

Answer: $\frac{2}{5}, -6$

33) _____

34) $2x^2 - 5x - 7 = 0$

Answer: $\frac{7}{2}, -1$

34) _____

35) $9x^2 - 7 = 18x$

Answer: $\frac{7}{3}, -\frac{1}{3}$

35) _____

36) $3x^2 + 15x + 18 = 0$

Answer: -3, -2

36) _____

Simplify. Assume that all variables represent positive numbers.

37) $\sqrt{64x^{11}}$

Answer: $8x^5\sqrt{x}$

37) _____

38) $\sqrt[8]{8x^{16}}$

Answer: $2x^2\sqrt[8]{2}$

38) _____

39) $\sqrt[3]{245x^2}$

Answer: $7x\sqrt[3]{5}$

39) _____

$$40) \sqrt{8k^7q^8}$$

Answer: $2k^3q^4\sqrt{2k}$

40) _____

$$41) 6\sqrt{2} + 3\sqrt{18}$$

Answer: $15\sqrt{2}$

41) _____

$$42) \sqrt{144} + \sqrt{98} + \sqrt{81} + \sqrt{18}$$

Answer: $10\sqrt{2} + 21$

42) _____

$$43) \sqrt{3} + 4\sqrt{12} - 6\sqrt{27}$$

Answer: $-9\sqrt{3}$

43) _____

$$44) \sqrt{3x^2} + x\sqrt{12}$$

Answer: $3x\sqrt{3}$

44) _____

$$45) \sqrt{6a} - 5\sqrt{24a} - 4\sqrt{150a}$$

Answer: $-29\sqrt{6a}$

45) _____

Multiply and simplify. Assume that all variables represent positive real numbers.

$$46) \sqrt{98} \cdot \sqrt{50}$$

Answer: 70

46) _____

$$47) \sqrt{3x^9} \cdot \sqrt{15x}$$

Answer: $3x^5\sqrt{5}$

47) _____

$$48) \sqrt{2}(\sqrt{10} + \sqrt{2})$$

Answer: $2\sqrt{5} + 2$

48) _____

$$49) (\sqrt{2} + \sqrt{5})(\sqrt{19} - \sqrt{5})$$

Answer: $\sqrt{38} + \sqrt{95} - \sqrt{10} - 5$

49) _____

$$50) (5\sqrt{13} + 9)(7\sqrt{13} + 4)$$

Answer: $491 + 83\sqrt{13}$

50) _____

$$51) (2\sqrt{7} + 6)^2$$

Answer: $64 + 24\sqrt{7}$

51) _____

Rationalize the denominator and simplify. Assume that all variables represent positive real numbers.

$$52) \sqrt{\frac{13}{3}}$$

Answer: $\frac{\sqrt{39}}{3}$

52) _____

$$53) \frac{\sqrt{7}}{\sqrt{11}}$$

$$53) \underline{\hspace{2cm}}$$

$$\text{Answer: } \frac{\sqrt{77}}{11}$$

$$54) \frac{5}{\sqrt{2}}$$

$$54) \underline{\hspace{2cm}}$$

$$\text{Answer: } \frac{5\sqrt{2}}{2}$$